

**Quiz I MTH 111, Spring 2017**

Ayman Badawi

**QUESTION 1.** 1. Given  $f_1 = (-5, 2)$ ,  $f_2 = (1, 2)$  are the foci of an ellipse and  $k = 8$  is the ellipse constant.

(i) Sketch roughly such ellipse.

(ii) Find all 4 vertices

(iii) Find the equation of the ellipse.

**QUESTION 2.** Let  $-12(y + 2) = (x - 3)^2$ .

(i) Find the focus and the vertex.

(ii) Find the equation of the the directrix line.

(iii) Sketch a rough graph of such parabola.

**Faculty information**Ayman Badawi, Department of Mathematics & Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.  
E-mail: [abadawi@aus.edu](mailto:abadawi@aus.edu), [www.ayman-badawi.com](http://www.ayman-badawi.com)

**Quiz II: MTH 111, Spring 2017**

Ayman Badawi

**QUESTION 1.** Consider the hyperbola  $\frac{(y-5)^2}{4} - \frac{(x+2)^2}{12} = 1$

- (i) Sketch roughly such hyperbola .
  
  
  
  
  
  
  
  
  
  
- (ii) Find the constant  $k$ .
  
  
  
  
  
  
  
  
  
  
- (iii) Find  $V_1, V_2$  (the two vertices of such hyperbola)
  
  
  
  
  
  
  
  
  
  
- (iv) Find  $F_1, F_2$  (the foci of such hyperbola)

**QUESTION 2.** Let  $v = \langle -4, 3 \rangle$ .

- (i) Find  $|v|$
  
  
  
  
  
  
  
  
  
  
- (ii) If  $(-8, 2)$  is the initial point of  $v$ , what is the terminal point of  $v$ ?
  
  
  
  
  
  
  
  
  
  
- (iii) Is  $w = \langle 2, 3 \rangle$  orthogonal (perpendicular) to  $v$ ? If not, then find the angle between them.

**Faculty information**

Ayman Badawi, Department of Mathematics & Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.  
E-mail: abadawi@aus.edu, www.ayman-badawi.com

**Quiz III: MTH 111, Spring 2017**

Ayman Badawi

**QUESTION 1.** (i) Let  $V = \langle 2, -2, -1 \rangle$ ,  $W = \langle 4, 3, 0 \rangle$ . Find  $Proj_W^V$ . Then find  $|Proj_W^V|$ .

(ii) Find a parametric equations of the line that passes through the two point:  $M = (1, 2, 5)$  and  $N = (6, -3, 7)$ .

(iii) Let  $M = (4, 2)$  and  $N = (-5, 0)$ . Draw the Projection vector M over N (i.e. draw  $Proj_N^M$ )

(iv) Find a parametric equations of the line that passes through the point  $M = (1, 2)$  and with direction vector  $\langle 5, 7 \rangle$ .

**Faculty information**

Ayman Badawi, Department of Mathematics & Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.  
E-mail: [abadawi@aus.edu](mailto:abadawi@aus.edu), [www.ayman-badawi.com](http://www.ayman-badawi.com)

**Quiz IV: MTH 111, Spring 2017**

Ayman Badawi

**QUESTION 1.** (i) Let  $L_1 : x = 2t - 1, y = t + 2, z = 3t$ ,  $L_2 : x = 2s - 5, y = s, z = -s + 6$ . If  $L_1$  intersects  $L_2$ , find the intersection point.

(ii) Find an equation of the plane that passes through  $(0, 1, 2)$ ,  $(-1, 2, 0)$ ,  $(4, 2, 1)$ .

(iii) Can we draw the vector  $v = \langle 3, -2, 1 \rangle$  inside the plane  $2x + y - 4z = 12$ ? EXPLAIN

**Faculty information**

Ayman Badawi, Department of Mathematics & Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.  
E-mail: abadawi@aus.edu, www.ayman-badawi.com

**Quiz V: MTH 111, Spring 2017**

Ayman Badawi

**QUESTION 1.** (i) Let  $P_1 : x + 2y - z = 4$ ,  $P_2 : -x - y + z = 2$ . If  $P_1$  intersects  $P_2$  find the intersection line.

(ii) Let  $P_1 : x + y + z = 2$ ,  $P_2 : -x - z = 4$ ,  $P_3 : -2x - 2y - z = 0$ . If the three planes intersect, what is the intersection?

**Faculty information**

Ayman Badawi, Department of Mathematics & Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.  
E-mail: abadawi@aus.edu, www.ayman-badawi.com

**Quiz VI: MTH 111, Spring 2017**

Ayman Badawi

**QUESTION 1.** find  $y'$  (Do not simplify)

(i)  $y = 3x^4 - 7x + 4$

(ii)  $y = \sqrt{3x+2} - \frac{5}{x} + 1$

(iii)  $y = 6(\sqrt[5]{(x^2 + 10x)^3}) - x$

(iv)  $\frac{x^6 + 4x^4 - 7}{x^3}$

**QUESTION 2.** Find the equation of the tangent line to the curve of  $f(x) = -4x^3 + 7x + 11$  when  $x = 2$ **Faculty information**Ayman Badawi, Department of Mathematics & Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.  
E-mail: abadawi@aus.edu, www.ayman-badawi.com

**Quiz VII: MTH 111, Spring 2017**

Ayman Badawi

**QUESTION 1.** find  $y'$  (Do not simplify)

(i)  $y = (\sqrt{x} + 3x)^3(4x - 2)^5$

(ii)  $y = (3x^2 - 6x + 3)^{10}(7x + 2)^6$  (*it is boring...enough of product formula*)

**QUESTION 2.** Let  $f(x) = x^3 - 3x^2 - 9x + 8$ For what values of  $x$  does  $f(x)$  increase?For what values of  $x$  does  $f(x)$  decrease?

Find all local minimum points and local maximum points.

Roughly, sketch the curve of  $f(x)$ **Faculty information**Ayman Badawi, Department of Mathematics & Statistics, American University of Sharjah, P.O. Box 26666, Sharjah, United Arab Emirates.  
E-mail: [abadawi@aus.edu](mailto:abadawi@aus.edu), [www.ayman-badawi.com](http://www.ayman-badawi.com)